

# An adaptive genetic algorithm for parameter estimation of biological oscillator models to achieve target quantitative system response

Martin Stražar · Miha Mraz · Nikolaj Zimic ·  
Miha Moškon

© Springer Science+Business Media Dordrecht 2013

**Abstract** Mathematical modeling has become an integral part of synthesizing gene regulatory networks. One of the common problems is the determination of parameters, which are a part of the model description. In the present work, we propose a customized genetic algorithm as a method to determine the parameters such that the underlying oscillatory system exhibits the target behavior. We propose a problem specific, adaptive fitness function evaluation and a method to quantify the effect of a single parameter on the system response. The properties of the algorithm are highlighted and confirmed on two test cases of synthetic biological oscillators.

**Keywords** Adaptive genetic algorithm · Biological oscillator · Gene regulatory networks · Parameter estimation

## 1 Introduction

In the recent years, notable improvement has been accomplished in understanding the component interactions in various living organisms, leading to improved and more accurate modeling techniques available in the fields of synthetic and systems biology (Alon 2007).

A common biological subsystem is an oscillating regulatory network responsible for maintaining the circadian rhythm which in turn affects the sleep-wake cycle, thermogenesis, feeding, glucose and lipid metabolism, energy balance, regulation of peripheral body clocks, respiratory

control, etc. Diseases such as diabetes, Alzheimer's disease, sleeping disturbances and various metabolic diseases are known to be caused by disruption in the oscillatory mechanism (Turek et al. 2005; Morton et al. 2005; Wu et al. 2006). Understanding the behavior of oscillatory systems is essential upon approaching such problems.

The dynamics of the oscillatory systems are well understood, as well as the conditions for the emergence of the necessary unstable limit cycle (Novák and Tyson 2008). Also, synthetic oscillators based on gene regulatory networks (GRNs) have been successfully realized both in prokaryotes (Elowitz and Leibler 2000) as well as in mammalian cells (Tigges et al. 2009). A fundamental problem in modeling synthetic GRNs is the uncertainty in the values of the model parameters (Lillacci and Khammash 2010, 2012) and the level of modeling complexity for a specific network. In Scheper et al. (1999) the authors show minimal required conditions for a biological oscillator model by treating various post-transcriptional processes as a single delay process. In order to achieve the targeted 24-h period they partly explore the parameter space while restricting the parameters within predefined boundaries.

In the present study we extend the concept of exploring the parameter space towards achieving a targeted system response, which is characterized by the frequency and amplitude of the resulting oscillations. We employ a customized, adaptive genetic algorithm which can be applied to an arbitrary oscillator model, based on delayed differential equations (DDEs) and is able to find globally optimal parameters that cause responses which can range over several orders of magnitude for both amplitude and frequency.

Various methods and tools aimed at optimizing and seeking the desired behavior of GRNs have been proposed.

---

M. Stražar (✉) · M. Mraz · N. Zimic · M. Moškon  
Faculty of Computer and Information Science, University  
of Ljubljana, Tržaska cesta 25, Ljubljana, Slovenia  
e-mail: martin.strazar@gmail.com

General methods rely on having a pre-established library of modular components and searching for the optimal network topology that would produce the desired response. Implementations (Rodrigo et al. 2007; Rodrigo and Jaramillo 2012) may employ a truth table for the desired function as an input and produce the optimal network topology as output using evolutionary techniques. Whether the resulting components would perform in a linear manner when wired together remains an open question due to observed non-modularity in living organisms (Hajimorad et al. 2011). François and Hakim (2004) perform a more specific study, where they define the characteristics of the desired response more precisely. Our approach is focused on a specific subgroup of networks in order to (a) take advantage of the knowledge about the expected system response and (b) provide quantitative answers about network parameters such that they can be used to aid the design decision while building such networks.

Genetic algorithms have long been used to tackle analytically intractable optimization problems in multidimensional parameter space (Chambers 2000). Recent developments in the field tend towards adaptive behavior of the algorithms. Examples include dynamic tuning of mutation rates, balancing the ratios between mutations and crossover or adapting the fitness function depending on the current state of the population. In Law and Szeto (2007), authors have demonstrated the advantages of mutation and crossover probabilities, proportional the fitness of an individual. Also, they have shown the importance of a single parameter influence on the overall fitness can be quantified by calculating its standard deviation. Summing up, less important parameters in less fit individuals tend to be subject to mutation with higher probability, while crossover is applied to fitter individuals more often. Using a similar method, the population of individuals in our case is replicated with a bias towards the fitter solutions.

The influence of each parameter in the resulting system response is quantified using the entropy function, an appropriate way to quantify determinism (Szendro et al. 2013). Repeatability is a measure of quantifying the determinism regarding an instance of evolution. It is defined as a probability that two independent evolutions will follow exactly the same path (Roy 2009). By performing multiple runs of the developed genetic algorithm, we derive the statistics for each parameter and quantify its influence on the resulting system response.

Various choices of mutation probabilities are discussed in (Smith and Fogarty 1996). Local maxima in the fitness landscapes are an emphasized problem of genetic algorithms. To be able to perform giant leaps in parameter space one should allow multiple alterations to be performed on candidate solutions. This can be achieved by allowing multiple mutations of parameters and/or usage of

crossover. That way, a significantly larger number of possible evolution scenarios are available (Roy 2009) and given enough time, the globally optimal solution will always take over the population (Szendro et al. 2013; Chambers 2000). Allowing multiple mutations and crossover cause faster escape from the local maxima as well as opening the possibility of beneficial joint mutations which are otherwise deleterious (Weinreich and Chao 2005). As we apply the algorithm to a specific family of problems, we assess the optimal choices for mutation probability and crossover method.

Adaptive behavior is further explored, using an adaptive fitness function. The performance gains caused by the usage of the population state dependent fitness evaluation are described in Farmani and Wright (2003). In addition, the authors introduce a concept of penalization of unfeasible solutions. We argue the performance gains of a problem specific, adaptive fitness function which also penalizes the unfeasible solutions. Evolutionary approaches towards tuning the response of biological circuits (Paladugu and Chickarmane 2006; Szendro et al. 2013; Fang et al. 2009) tend to use generic fitness measures (e.g. non-linear least squares error), limiting the solution space. The problem specificity of the fitness function gives us the advantage of finding equivalently fit solutions in larger solution space, since it is not limited by absolute values of the resulting system response.

The resulting set of parameter values guarantees the desired system response for a given model of a biological oscillator, offering a quantitative insight of the conditions that have to be met on the design level. The manipulation of parameter values of a GRN is to some degree already achievable in vivo. Examples include engineering synthetic ribosome binding sites to influence translation efficiency (Salis et al. 2009), modifying the upstream promoter sequences to alter the transcription rate (Rhodius et al. 2012), using transcription factor proteins with different degree of cooperativity (Dill et al. 1993) or degradation tags to accelerate the protein degradation (Butz et al. 2011). Studies that rely on modifying the temporal behavior of rhythmic systems ought to make use of the quantitative knowledge of parameter values to achieve the desired effects (Mackey and Glass 1977; Morton et al. 2005; Wu et al. 2006). A concept similar to our was also performed in vivo (Yokobayashi et al. 2002) in which the authors deliberately induce mutations during the cloning process to demonstrate the achievable change in protein–protein as well as protein–DNA interactions, which confirms the practical applicability of our approach.

Section 2 introduces the computational framework used in the study. Section 3 presents results achieved on two different models of biological oscillators, which are discussed in Section 4.

## 2 Framework

### 2.1 Algorithm overview

A common way to model GRNs are ordinary differential equations (ODEs), which describe the change of a given species concentration in an infinitesimal interval of time. In general terms, the form of such description is

$$\frac{\delta S_i}{\delta t} = f(S_1(t), S_2(t), \dots, S_n(t), p_1, p_2, \dots, p_m) \quad (1)$$

where  $S_i$  are the observed chemical species,  $S_1(t), S_2(t), \dots, S_n(t)$  is the system state vector and  $p_1, p_2, \dots, p_m$  is a vector of parameters, which determine the system behavior. As processes in the cell span over multiple time scales (Scheper et al. 1999), the description can be altered to a system of DDEs:

$$\frac{\delta S_i}{\delta t} = f(S_1(t - \tau_1), S_2(t - \tau_2), \dots, S_n(t - \tau_n), p_1, p_2, \dots, p_m)$$

where the delays with which species affect the system are given by  $\tau_1, \tau_2, \dots, \tau_n$ . The vector of parameters and the vector of time delays uniquely describe the response of a DDE system. A combination of their values represent a candidate solution.

### 2.2 Fitness evaluation

Considering the system response as a discrete time signal, we used its standard deviation along the  $y$  axis as an approximation to the amplitude  $A$ . The frequency  $f$  was in turn detected using the discrete fast Fourier transform (FFT). Furthermore, the *unfeasible* candidate solutions that reached a stable steady state could be detected. By acquiring the two values, the fitness of an individual candidate solution  $C_i$  was determined by computing the relative error ratio against targeted amplitude  $A$  and frequency  $f$ :

$$F(C_i) = \begin{cases} \Delta_a \cdot \Delta_f & \text{if } C_i \text{ is feasible,} \\ X + \Delta_a \cdot \Delta_f & \text{else;} \end{cases} \quad (3)$$

where  $\Delta_a = \|(A_i - A)\|/A$  and  $\Delta_f = \|(f_i - f)\|/f$  present obtained candidate solution response errors regarding the target amplitude and frequency values respectively. In case of an unfeasible solution, a regularization term  $X$  (empirically defined  $10^9$ ) was added to the resulting fitness in order to partition population on the feasibility of solutions. The approach agrees with the method proposed in Farmani and Wright (2003), where unfeasible solutions are still kept in the population for potential adjustments. This turns out to be particularly important when feasible solutions are located in a very narrow parameter range and eliminating

unfeasible solutions would cause the population to effectively decrease.

An efficient approach in exploring the parameter space is to make large steps in the earlier phases and performing local optimization afterwards. We further improved the algorithm by using an adaptive fitness function. In the beginning, candidate fitness is evaluated such that:

$$F(C_i) = \begin{cases} \Delta_f & \text{if } C_i \text{ is feasible;} \\ X + \Delta_f & \text{else;} \end{cases} \quad (4)$$

After the evolution finds a candidate solution with sufficiently small frequency error (empirically defined as 1 %), fitness evaluation method changes to Eq. 3. Thus, by first adjusting the frequency and then performing local optimization considering both frequency and amplitude, the population proved to converge to the optimum value in a smaller number of steps. The approach mimics the simulated annealing algorithm (Vecchi 1987) in a sense of performing large steps in the beginning and stems from the fact that some parameters mainly influence either amplitude or frequency while others influence both amplitude and frequency (see Sect. 3).

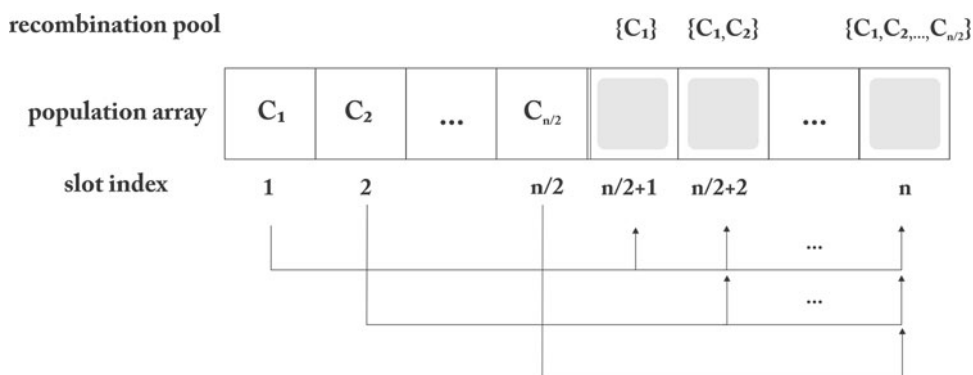
### 2.3 Selection and reproduction

The candidate solutions are afterwards sorted based on the ascending value of  $F(C_i)$ . Only the top half thus comprises the reproduction pool, while the lower half is discarded and slots are available for new candidate solutions. Random pairs of candidates are selected from the reproduction pool and their parameter vectors recombined into one with an equal probability for each component coming from either of parents (n-point crossover). This ensures the ability to make large steps in parameter space and avoid local maxima (Chambers 2000).

To bias the selection towards fitter candidates, the reproduction pool grows dynamically during the crossover step for each unoccupied candidate solution slot. As the algorithm iterates through slots in previously discarded bottom half of the population, a candidate is added to the current reproduction pool when producing each new individual. In this way, fitter candidates will be in the reproduction pool sooner and their components will have higher probability to appear in the resulting new population. This modification appeared to produce better results and was based on the results obtained in (Law and Szeto 2007) and is explained in more detail on Fig. 1.

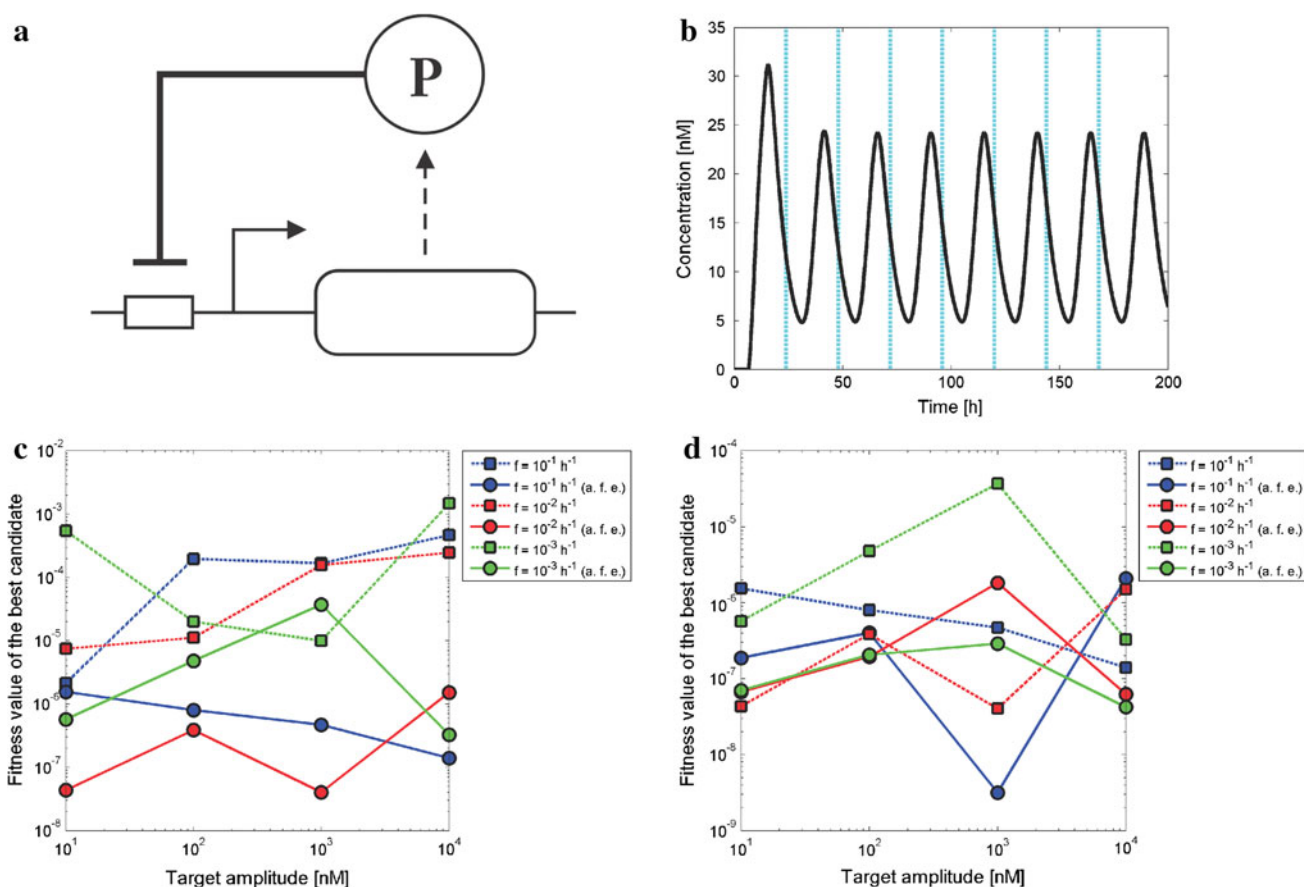
Mutations are applied to the parameter vector  $p_{i,1}, p_{i,2}, \dots, p_{i,l}$  of each candidate solution  $C_i$  with the probability proportional to the parameter vector length  $l$  (Back 1992), such that

$$p_{i,j} = p_{i,j} + G(0, 1) \quad (5)$$



**Fig. 1** The proposed biased selection method. After the fitness of each individual candidate solution  $C_i$  is evaluated, the candidates are sorted and the bottom half (gray) is discarded. The resulting empty slots in the population array are then occupied by new candidates, which are derived by performing crossover of candidates from the recombination pool. The former is dynamic, in a sense that new

candidate solutions are added for each slot in accordance with their fitness value. For example, the new candidate on index  $n/2 + 1$  is a mutated best candidate, new candidate on index  $n/2 + 2$  is a recombination from candidates  $C_1$  and  $C_2$ , while at the last index  $n$  the resulting candidate is derived from a random pair of candidates from the whole upper half  $C_1, C_2, \dots, C_n$



**Fig. 2** **a** Schematic representation of a single repressor oscillator model; **b** Simulation of optimal solution of parameter space search for target amplitude  $A = 16$  nM and frequency  $f = 0.042 h^{-1}$ . Parameters:  $\tau = 12.906$  h,  $r_M = 8.025$  nM/h,  $r_P = 15.884$  nM/h,  $q_M = 0.045$ ,  $q_P = 0.067$ ,  $m = 2.69$ ,  $h = 2.083$  and  $k = 9.88$ . 24-h periods are marked

with a cyan dashed line. **c** Comparison of parameters space investigation for amplitudes and frequencies of different orders of magnitude with (circles) and without crossover (squares); **d** Comparison of parameters space investigation for amplitudes and frequencies of different orders of magnitude with (circles) and without adaptive fitness evaluation (squares)

where  $G$  is a normally distributed random variable with zero mean and SD of one. To ensure that the quality of solutions monotonically increases, the current fittest candidate is never discarded and remains unchanged (elitism) in the next evolution cycle (Chambers 2000).

### 3 Results

#### 3.1 Oscillator model

The proposed approach was evaluated using the oscillator model, based on a negative feedback loop proposed in (Scheper et al. 1999) and schematically depicted in Fig. 2a. It can be described with a DDE system:

$$\frac{\delta M_i}{\delta t} = \frac{r_m}{1 + \left(\frac{P(t)}{k}\right)^h} - q_m \cdot M_i(t) \quad (6)$$

$$\frac{\delta M_i}{\delta t} = r_p \cdot M(t - \tau)^m + q_p \cdot P(t) \quad (7)$$

where the system state is composed of  $M$  as the mRNA concentration and  $P$  as the concentration of the repressor protein. System parameters that we have to determine are mRNA transcription rate  $r_m$ , protein translation rate  $r_p$ , mRNA degradation rate  $q_m$ , protein degradation rate  $q_p$ , scaling constant for the repressor protein  $k$ , mRNA non-linearity coefficient  $m$ , repressor protein cooperativity coefficient  $h$  and time delay between transcription and translation  $\tau$ . To further exploit the a priori knowledge about the system, constraints on parameter values are employed. This helps us narrow down the search space and increase convergence speed. In Scheper et al. (1999), it is argued that described system can exhibit oscillatory behavior if and only if  $\tau > 0$ . On top of that, we constrained the degradation rates for both protein and mRNA such that  $q_m, q_p < 1$  and non-linearity coefficients  $m, h > 1$ .

After reaching the unstable steady state, the system exhibits an oscillatory response. We performed a search for the target amplitude of 16 nM and target period of 24 h (frequency  $0.042 \text{ h}^{-1}$ ) obtained in (Scheper et al. 1999) and found another equivalent solution in the parameter space (Fig. 2b). The observations and conditions for oscillations observed in (Scheper et al. 1999; Novák and Tyson 2008) apply to the resulting parameter vector as well, indicating there is more than one point in the solution space producing equivalent system response in terms of amplitude and frequency.

Running the evolutions for a range of amplitudes and frequencies spanning various orders of magnitude, the search method returned results with error values of the order  $10^{-5}$  on average. To achieve optimal results, we adjusted and tested different properties of the proposed

algorithm. Crossover of different parameter values proves beneficial for some problems while not for the others (Chambers 2000). As the system response qualitatively depends on the ratios among parameter vector components (Novák and Tyson 2008), conservation of fit subparts of parameter vectors proves beneficial. Figure 2c shows the comparison of evolution runs with and without using crossover. The fitness function value after running evolution runs with 150 population iterations was clearly lower by more than one order of magnitude for a large majority of evolution runs when using crossover, confirming the feasibility of its use for our particular group of problems.

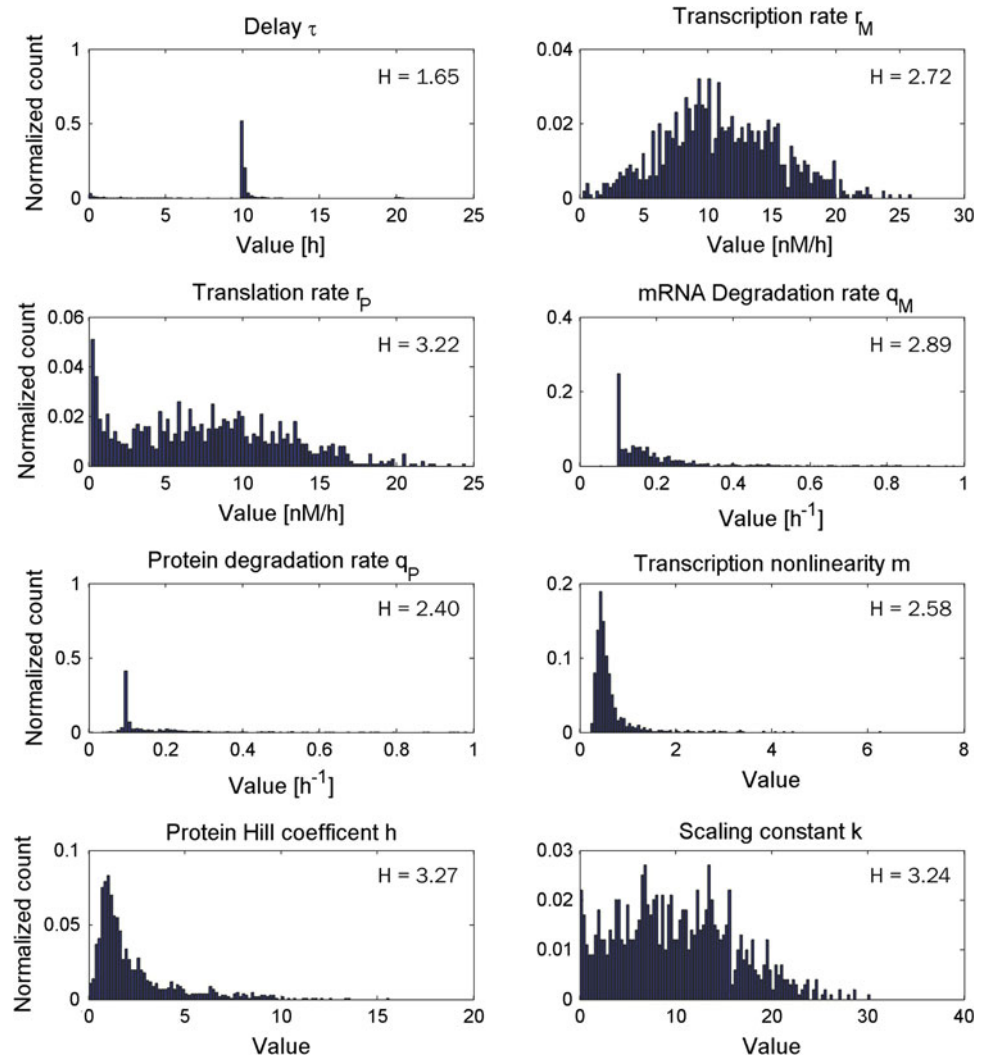
In a similar manner, we evaluated the use of the proposed adaptive fitness evaluation function explained in Sect. 2. By first evaluating only the frequency of the system response and after the population exceeded a predetermined error threshold (in our case  $< 1\%$ ), we started with the fitness evaluation function in Eq. 4 until reaching the target frequency accuracy and only then proceeding with Eq. 3. Thus evolution runs were able to achieve faster convergence. Consequently, the global error value is lower for evolutions using the adaptive error evaluation function, which is clearly seen on Fig. 2d.

The hypothesis posed in Sect. 2 that some parameters influence either amplitude or frequency while others influence both was directly tested. Running various single oscillator simulations with gradually tuning two chosen parameters, we discover that both transcription rate  $r_m$  and translation rate  $r_p$  only affect the amplitude (Fig. 4c), while none of them affects the resulting frequency (Fig. 4d). This fact explains the advantage of the proposed adaptive fitness evaluation function, which offers the possibility to first find a solution with a satisfying frequency accuracy and subsequently tuning the parameters which influence amplitude without affecting the obtained frequency. This is an important result since it not only decreases the search time and reduces the fitness function dimensionality, but also improves the overall quality of the end solution.

To investigate whether the proposed algorithm is able to find a global optimum, we performed runs of 1,000 independent evolutions with the same initial values (Fig. 3). The resulting statistics for the final value of each individual parameter are modal distributions with a clearly distinguishable peak, indicating the algorithm ends the search near the global optimum with high probability.

As shown in Law and Szeto (2007), the amount of information carried by an individual parameter is directly proportional to its SD across the population of candidate solutions. We calculate the entropy of parameter value distribution, similarly as proposed in François and Hakim (2004) as a convenient way to quantify evolution determinism. For each individual parameter  $p_j$  a histogram with  $b$  bins is computed and its entropy is calculated

**Fig. 3** Distribution of individual parameter values for 1,000 independent evolution runs with normalized counts and calculated entropies using Eq. 8



$$H(p_j) = \sum_{k=1}^b c_{k,j} \cdot \log(c_{k,j}) \tag{8}$$

where  $c_{k,j}$  presents the probability of parameter  $j$  having the value in the interval of the bin  $k$ .

As can be observed from the results obtained in Fig. 3, the parameter that most notably influences the overall solution fitness (bears least entropy in value distribution) is time delay  $\tau$  [consistent with findings in Scheper et al. (1999) and Novák and Tyson (2008)], while the influence of the scaling constant  $k$  is among the least noticeable. Running the simulations by adjusting these two parameters while keeping the rest constant (at their calculated mean values) clearly shows the time delay  $\tau$  influences both amplitude (Fig. 4a) and frequency (Fig. 4b), while the influence of  $k$  on both is negligible. Thus, the entropy proves an effective measure to quantify individual parameter importance for the measured response and the results can be applied in the design process of synthetic in vivo biological circuits.

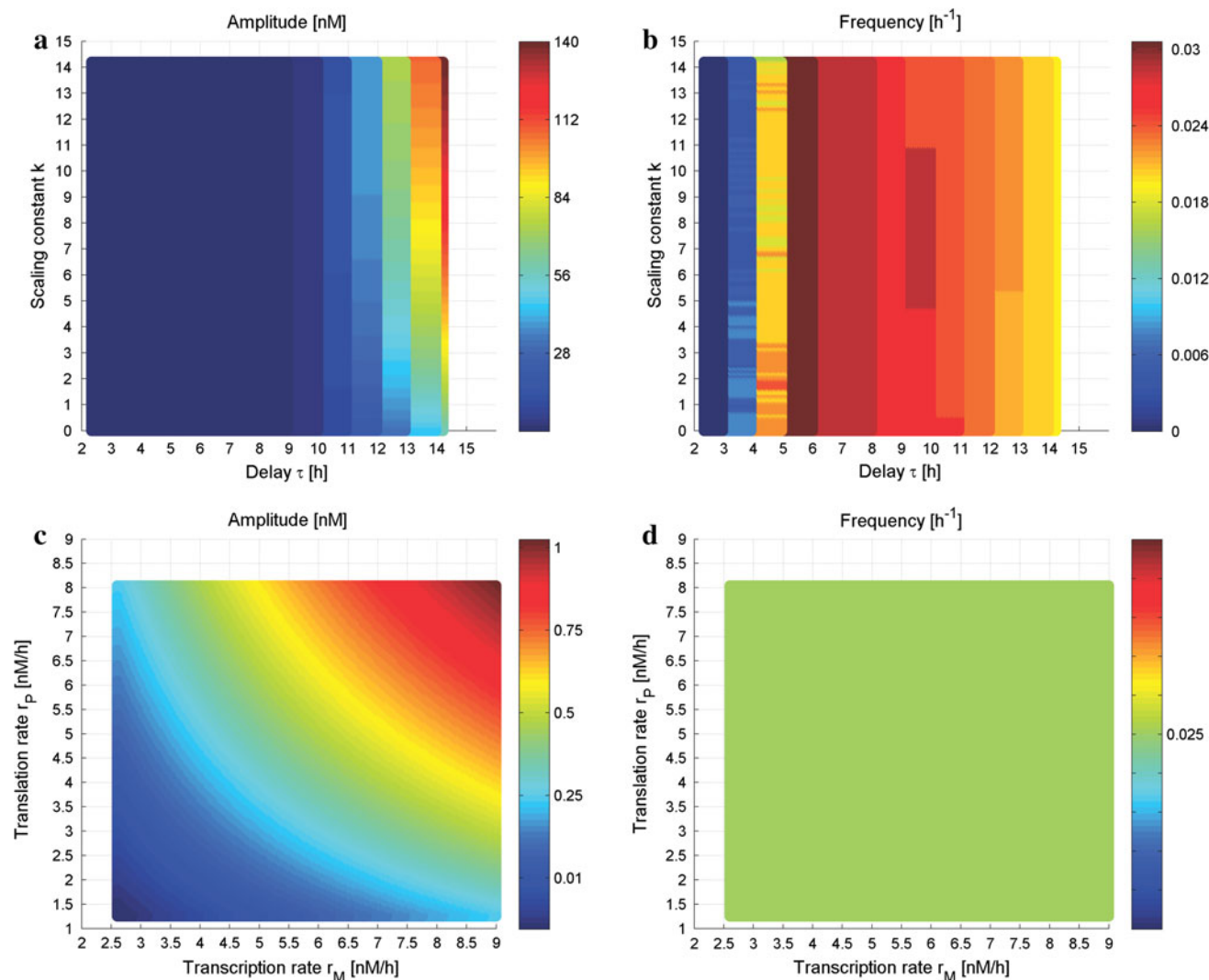
### 3.2 Repressilator model

Proposed approach was tested on the model with a larger number of interacting genes (Elowitz and Leibler 2000) in order to investigate its scalability. The general repressilator model is composed of an odd number of repressors (Fig. 5a) such that

$$\frac{\delta M_x}{\delta t} = -\gamma \cdot M_x(t) + \frac{\alpha_1}{1 + \left(\frac{P_y(t)}{k}\right)^h} + \alpha_0 \tag{9}$$

$$\frac{\delta P_x}{\delta t} = -\eta \cdot P_x(t) + \beta \cdot M_x(t - \tau) \tag{10}$$

where  $x, y \in 1, \dots, N$  is the repressor protein index,  $M_x$  is the mRNA concentration of the corresponding repressor  $P_x$ . Parameters that have to be determined are mRNA degradation rate  $\gamma$ , maximal (unrepressed) mRNA production rate  $\alpha_1$ , promoter leakage  $\alpha_0$ , repressor scaling constant  $k$ , cooperativity coefficient  $h$ , protein degradation rate  $\eta$ , protein production rate  $\beta$  and transcription–translation time delay  $\tau$ . In



**Fig. 4** Effect on resulting amplitude and frequency of the single repressor oscillator model for tuning of the two parameters for a range  $[\mu - \sigma, \mu + \sigma]$  where  $\mu$  and  $\sigma$  are the mean and the standard deviations of parameter values obtained from a run of 1,000 parallel

simulations (Fig. 3). Other parameters are kept constant at their mean values. **a** Effect on amplitude by tuning parameters  $\tau$  and  $k$ . **b** Effect on frequency by tuning parameters  $\tau$  and  $k$ . **c** Effect on amplitude for parameters  $r_M$  and  $r_P$ . **d** Effect on frequency for parameters  $r_M$  and  $r_P$

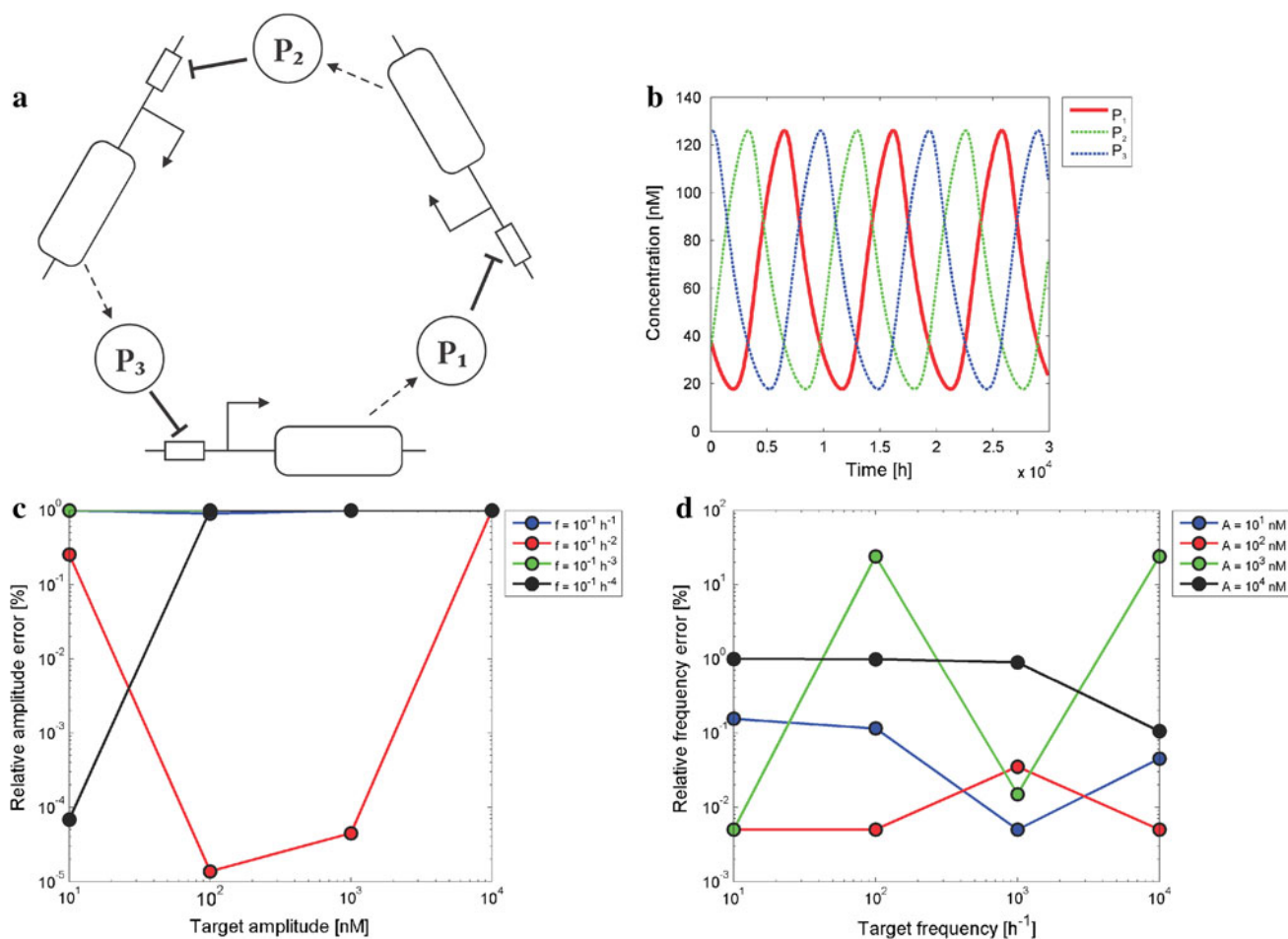
case of the repressator with three repressors, the model is composed of six equations and nine parameters. An example simulation run of the repressator is shown on Fig. 5b. The parameters found after 150 generations cause oscillating behaviour with shifted phases among the three repressor proteins as anticipated.

As the amplitude and frequency of the oscillations are mainly dependent on the stability of the protein (Elowitz and Leibler 2000), we modified the model such that

$$\frac{\delta M_x}{\delta t} = -\gamma \cdot M_x(t) + \frac{\alpha_1}{1 + \left(\frac{P_y(t)}{k_x}\right)^h} + \alpha_0 \tag{11}$$

$$\frac{\delta P_x}{\delta t} = -\eta_x \cdot P_x(t) + \beta_x \cdot M_x(t - \tau) \tag{12}$$

Here the scaling constant  $k_x$ , protein degradation rates  $\eta_x$  and translation rates  $\beta_x$  are unique for each protein in the circuit, which increases the number of parameters to 15. Results in Fig. 5c, d present relative error margins for end results of simulations for various orders of magnitude for targeted amplitudes and frequencies. The errors are below 0.01 % in majority of cases, which underlines the feasibility and the scalability of the approach. Also, by tuning separately a subgroup of parameters  $\beta_x, \eta_x, k_x$  while keeping other parameters equal for each of the three components of the network, we show that the frequency and amplitude response of the repressator can be adjusted with the choice of interacting repressors' properties alone. This observation is constant with experimental studies (Elowitz and Leibler 2000) while quantifying the observed information as well.



**Fig. 5** **a** Schematic representation of the repressilator circuit. **b** Simulation of optimal solution of parameter space search for target amplitude  $A = 100$  and frequency  $f = 0.0001 \text{ h}^{-1}$ . Parameters used:  $\alpha_0 = 2.288^{-7} \text{ nM/h}$ ,  $\alpha_1 = 1.94 \text{ nM/h}$ ,  $\beta = 0.0002 \text{ nM/h}$ ,  $n = 4.199$ ,  $\gamma = 0.0005$ ,  $\eta = 0.007$ ,  $k = 45.313$ ,  $\tau = 0.09 \text{ h}$ . **c** Comparison of parameters space investigation for amplitudes and frequencies of varying orders

using Eqs. 9 and 10 (circles) or Eqs. 11 and 12 (squares). The y axis shows the relative amplitude error regarding the target amplitude. **d** Comparison of parameters space investigation for amplitudes and frequencies of varying orders of magnitude Eqs. 9 and 10 (circles) or Eqs. 11 and 12 (squares). The y axis shows the relative frequency error regarding the target frequency

## 4 Discussion

We have developed a method to explore the parameter space and performed a thorough parameter analysis for biological oscillator circuit models with a predefined topology. By making use of a priori knowledge of the observable system dynamics, we were able to further narrow the parameter values while retaining the ability of finding the values that lead to the desired system response. The former is represented by a combination of oscillating amplitude and frequency which can be adjusted over a wide range of orders of magnitude. We efficiently applied digital signal processing methods to analyze the oscillating behavior to evaluate the candidate solutions.

The proposed genetic algorithm proved effective for two different types of models and wide range of input parameters which indirectly confirmed its scalability. Comparing

the evolution with and without using crossovers, we have concluded that it significantly improves the end result as a way of retaining fit subparts of parameter vectors. It reinforces the fact that the systems response is mainly dependent on ratios between different parameters. Hence the fitter combinations of a subgroup of parameters can be efficiently spread over candidate solutions pool (population). We included state-of-the-art developments in genetic algorithms by allowing multiple mutations, biased crossover towards fitter candidate solutions, partitioning the solutions on their feasibility and proposed a new approach of a problem dependent adaptive fitness evaluation, based on the effect of single parameters to the resulting system response.

Being able to perform giant leaps in parameter space by means of crossover and multiple mutations, the system successfully converges towards the optimal solution and



avoids local maxima. Due to the use of elitism, convergence is always monotonic. By running various simulations with equal inputs, the simulations converged towards a vector with a clear, modal statistical distribution for each component (parameter). As the starting candidate solutions are purely random, we assert the vector of means is the global optimum with high probability. Each parameter was assigned an entropy value, which allowed us to determine and quantify the amount of information and the importance for a single parameter.

As we have shown the approach is applicable to oscillating systems with varying complexity, we turn towards the applicability of its results. By assessing separately the tunable parameters used in the repressilator model while keeping the remaining untunable parameters constant, we conclude amplitude and frequency of oscillators can be adjusted only by altering the protein dependent parameters. Thus, the resulting vector of parameter values can be used to aid the decisions during design and experimentation of in vivo synthesis and analysis of biological circuits.

**Acknowledgements** The research was supported by the scientific research programme Pervasive Computing (P2-0359) financed by Slovenian Research Agency in years from 2009 to 2012. Results presented here are in scope of Ph.D. thesis that is being prepared by Martin Stražar.

## References

- Alon U (2007) An introduction to systems biology: design principles of biological circuits. Chapman & Hall/CRC, New York
- Back T (1992) Self-adaptation in genetic algorithms. In: Towards a practice of autonomous systems proceedings of the first European conference on artificial life. MIT Press, Cambridge, pp 263–271
- Butz M, Neuenschwander M, Kast P, Hilvert D (2011) An N-terminal protein degradation tag enables robust selection of highly active enzymes. *Biochem Cell Biol* 50(40):8594–8602
- Chambers LD (2000) The practical handbook of genetic algorithms: applications. Chapman and Hall/CRC, Perth
- Dill KA, Fiebig KM, Chan HS (1993) Cooperativity in protein-folding kinetics. *Proc Natl Acad Sci USA* 90(5):1942–1946
- Elowitz MB, Leibler S (2000) A synthetic oscillatory network of transcriptional regulators. *Nat Biotechnol* 403(6767):335–338
- Fang F, Ni BJ, Yu HQ (2009) Estimating the kinetic parameters of activated sludge storage using weighted non-linear least-squares and accelerating genetic algorithm. *Water Res* 43(10):2595–2604
- Farmani R, Wright J (2003) Self-adaptive fitness formulation for constrained optimization. *IEEE Trans Evol Comput* 7(5):445–455
- François P, Hakim V (2004) Design of genetic networks with specified functions by evolution in silico. *Proc Natl Acad Sci USA* 101(2):580–585
- Hajimorad M, Gray PR, Keasling JD (2011) A framework and model system to investigate linear system behavior in *Escherichia coli*. *J Biol Eng* 5(1):3
- Law N, Szeto K (2007) Adaptive genetic algorithm with mutation and crossover matrices. In: Proceedings of the 20th international joint conference on artificial intelligence, Hyderabad, India, pp 2330–2333
- Lillacci G, Khammash M (2010) Parameter estimation and model selection in computational biology. *PLoS Comput Biol* 6(3):696
- Lillacci G, Khammash M (2012) A distribution matching method for parameter estimation and model selection in computational biology. *Int J Robust Nonlinear Control* 22:1065–1081
- Mackey M, Glass L (1977) Oscillation and chaos in physiological control systems. *Sci Agric* 197(4300):287–289
- Morton AJ, Wood NI, Hastings MH, Hurelbrink C, Barker Ra, Maywood ES (2005) Disintegration of the sleep-wake cycle and circadian timing in Huntington's disease. *J Neurosci* 25(1):157–163
- Novák B, Tyson JJ (2008) Design principles of biochemical oscillators. *Nat Rev Mol Cell Biol* 9(12):981–991
- Paladugu S, Chickarmane V (2006) In silico evolution of functional modules in biochemical networks. *Syst Biol* 153(4):223–236
- Rhodius VA, Mutalik VK, Gross CA (2012) Predicting the strength of UP-elements and full-length *E. coli*  $\sigma$ E promoters. *Nucl Acids Res* 40(7):2907–2924
- Rodrigo G, Jaramillo A (2012) AutoBioCAD: full biodesign automation of genetic circuits. *ACS Synth Biol*. doi:10.1021/sb300084h
- Rodrigo G, Carrera J, Jaramillo A (2007) Genetdes: automatic design of transcriptional networks. *Bioinformatics (Oxford, England)* 23(14):1857–1858
- Roy SW (2009) Probing evolutionary repeatability: neutral and double changes and the predictability of evolutionary adaptation. *PLoS One* 4(2):e4500
- Salis HM, Mirsky EA, Voigt CA (2009) Automated design of synthetic ribosome binding sites to control protein expression. *Nature Biotechnol* 27(10):946–950
- Scheper T, Klinkenberg D, Pennartz C, van Pelt J (1999) A mathematical model for the intracellular circadian rhythm generator. *J Neurosci* 19(1):40–47
- Smith J, Fogarty T (1996) Self adaptation of mutation rates in a steady state genetic algorithm. In: Proceedings of IEEE international conference on evolutionary computation, pp 318–323
- Szendro IG, Franke J, de Visser JAGM, Krug J (2013) Predictability of evolution depends nonmonotonically on population size. *Proc Natl Acad Sci USA* 110(2):571–576
- Tigges M, Marquez-Lago TT, Stelling J, Fussenegger M (2009) A tunable synthetic mammalian oscillator. *Nature* 457(7227):309–312. doi:10.1038/nature07616, URL <http://www.ncbi.nlm.nih.gov/pubmed/19148099>
- Turek FW, Joshi C, Kohsaka A, Lin E, Ivanova G, McDearmon E, Laposky A, Losee-Olson S, Easton A, Jensen DR, Eckel RH, Takahashi JS, Bass J (2005) Obesity and metabolic syndrome in circadian Clock mutant mice. *Science (New York, NY)* 308(5724):1043–1045
- Vecchi MP, Kirkpatrick S, Gelatt CD (1987) Optimization by simulated annealing, vol 220. *Sci N Ser* 220(4598):671–680
- Weinreich DM, Chao L (2005) Rapid evolutionary escape by large populations from local fitness peaks is likely in nature. *Evolution* 59(6):1175–1182
- Wu YH, Fischer DF, Kalsbeek A, Garidou-Boof ML, van der Vliet J, van Heijningen C, Liu RY, Zhou JN, Swaab DF (2006) Pineal clock gene oscillation is disturbed in Alzheimer's disease, due to functional disconnection from the "master clock". *FASEB J* 20(11):1874–1876
- Yokobayashi Y, Weiss R, Arnold FH (2002) Directed evolution of a genetic circuit. *Proc Natl Acad Sci USA* 99(26):16587–16591